
Dong Yuan, Yun Yang, Xiao Liu, Jinjun Chen
Faculty of Information and Communication Technologies,
Swinburne University of Technology
Hawthorn, Melbourne, Australia 3122
{dyuan, yyang, xliu, jchen}@swin.edu.au

Abstract
Many scientific workflows are data intensive where a large volume of intermediate datasets is generated during their execution. Some valuable intermediate datasets need to be stored for sharing or reuse. Traditionally, they are selectively stored according to the system storage capacity, determined manually. As doing science on cloud has become popular nowadays, more intermediate datasets in scientific cloud workflows can be stored by different storage strategies based on a pay-as-you-go model. In this paper, we build Intermediate data Dependency Graph (IDG) from the data provenances in scientific workflows. With IDG, deleted intermediate datasets can be regenerated, and as such we develop a novel algorithm that can find a minimum cost storage strategy for the intermediate datasets in scientific cloud workflows systems. The strategy achieves the best trade-off of computation cost and storage cost by automatically storing the most appropriate intermediate datasets in the cloud storage. This strategy can be utilised on demand as a minimum cost benchmark for all other intermediate datasets storage strategies in the cloud. We utilise Amazon clouds’ cost model and apply the algorithm to general random as well as specific astrophysics pulsar searching scientific workflows for evaluation. The results show that benchmarking effectively demonstrates the cost effectiveness over other representative storage strategies.

1. Introduction

Scientific applications are usually complex and data-intensive. In many fields, like astronomy [17], high-energy physics [26] and bioinformatics [29], scientists need to analyse terabytes of data either from existing data resources or collected from physical devices. The scientific analyses are usually computation intensive, hence taking a long time for execution. Workflow technologies can be facilitated to automate these scientific applications. Accordingly, scientific workflows are typically very complex. They usually have a large number of tasks and need a long time for execution. During the execution, a large volume of new intermediate datasets will be generated [18]. They could be even larger than the original dataset(s) and contain some important intermediate results. After the execution of a scientific workflow, some intermediate datasets may need to be stored for future use because: 1) scientists may need to re-analyse the results or apply new analyses on the intermediate datasets; 2) for collaboration, the intermediate results may be shared among scientists from different institutions and the intermediate datasets can be reused. Storing valuable intermediate datasets can save their regeneration cost when they are reused, not to mention the waiting time saved for regeneration. Given the large size of the datasets, running scientific workflow applications usually need not only high performance computing resources but also massive storage [18].

Nowadays, popular scientific workflows are often deployed in grid systems [26] because they have high performance and massive storage. However, building a grid system is extremely expensive and it is normally not open for scientists all over the world. The emergence of cloud computing technologies offers a new way to develop scientific workflow systems in which one research topic is cost-effective strategies for storing intermediate datasets.

In late 2007 the concept of cloud computing was proposed [33] and it is deemed as the next generation of IT platforms that can deliver computing as a kind of utility [14]. Foster et al. made a
comprehensive comparison of grid computing and cloud computing [20]. Cloud computing systems provide high performance and massive storage required for scientific applications in the same way as grid systems, but with a lower infrastructure construction cost among many other features, because cloud computing systems are composed of data centres which can be clusters of commodity hardware [33]. Research into doing science and data-intensive applications on the cloud has already commenced [27], such as early experiences like Nimbus [23] and Cumulus [32] projects. The work by Deelman et al. [19] shows that cloud computing offers a cost-effective solution for data-intensive applications, such as scientific workflows [22]. Furthermore, cloud computing systems offer a new model that scientists from all over the world can collaborate and conduct their research together. Cloud computing systems are based on the Internet, and so are the scientific workflow systems deployed in the cloud. Scientists can upload their data and launch their applications on the scientific cloud workflow systems from everywhere in the world via the Internet, and they only need to pay for the resources that they use for their applications. As all the data are managed in the cloud, it is easy to share data among scientists.

Scientific cloud workflows are deployed in a cloud computing environment, where all the resources need to be paid for use. For a scientific cloud workflow system, storing all the intermediated datasets generated during workflow executions may cause a high storage cost. On the contrary, if we delete all the intermediate datasets and regenerate them every time when needed, the computation cost of the system may well be very high too. The intermediate datasets storage strategy is to reduce the total cost of the whole system. The best way is to find a balance that selectively store some popular datasets and regenerate the rest of them when needed [8] [36] [38]. Some strategies have already been proposed to cost-effectively store the intermediate data in scientific cloud workflow systems [36] [38].

In this paper, we propose a novel algorithm that can calculate the minimum cost for the intermediate datasets storage in scientific cloud workflow systems. The intermediate datasets in scientific cloud workflows often have dependencies. Along workflow execution, they are generated by the tasks. A task can operate on one or more datasets and generate new one(s). These generation relationships are a kind of data provenance. Based on the data provenance, we create an Intermediate data Dependency Graph (IDG), which records the information of all the intermediate datasets that have ever existed in the cloud workflow system, no matter whether they are stored or deleted. With the IDG, we know how the intermediate datasets are generated and can further calculate their generation cost. Given an intermediate dataset, we divide its generation cost by its usage rate, so that this cost (the generation cost per unit time) can be compared with its storage cost per time unit, where a dataset’s usage rate is the time between every usage of this dataset that can be obtained from the system logs. Then we can decide whether an intermediate dataset should be stored or deleted in order to reduce the system cost. However, cloud computing environment is very dynamic, where the usages of intermediate datasets may change from time to time. Given the historic usages of the datasets in an IDG, we propose a Cost Transitive Tournament Shortest Path (CTT-SP) based algorithm that can find the minimum cost storage strategy of the intermediate datasets on demand in scientific cloud workflow systems. This minimum cost can be utilised as a benchmark to evaluate the cost effectiveness of other intermediate datasets storage strategies.

The remainder of this paper is organised as follows. Section 2 gives a motivating example of scientific workflow and analyses the research problems. Section 3 introduces some important related concepts and the cost model of intermediate datasets storage in the cloud. Section 4 presents the detailed minimum cost algorithms. Section 5 demonstrates the simulation results and
the evaluation. Section 6 discusses the related work. Section 7 is a discussion about the data transfer cost among cloud service providers. Section 8 addresses our conclusions and future work.

2. Motivating example and problem analysis

2.1 Motivating example

Scientific applications often need to process a large amount of data. For example, Swinburne Astrophysics group has been conducting pulsar searching survey using the observation data from Parkes Radio Telescope, which is one of the most famous radio telescopes in the world [4]. Pulsar searching is a typical scientific application. It contains complex and time consuming tasks and needs to process terabytes of data. Figure 1 depicts the high level structure of a pulsar searching workflow, which is currently running on Swinburne high performance supercomputing facility [6].

![Figure 1. Pulsar searching workflow](image)

At the beginning, raw signal data from Parkes Radio Telescope are recorded at a rate of one gigabyte per second by the ATNF [3] Parkes Swinburne Recorder (APSR) [2]. Depends on different areas in the universe that the scientists want to conduct the pulsar searching survey, the observation time is normally from 4 minutes to one hour. Recording from the telescope in real time, these raw data files have data from multiple beams interleaved. For initial preparation, different beam files are extracted from the raw data files and compressed. They are 1GB to 20GB each in size, depends on the observation time. The beam files contain the pulsar signals which are dispersed by the interstellar medium. De-dispersion is to counteract this effect. Since the potential dispersion source is unknown, a large number of de-dispersion files needs to be generated with different dispersion trials. In the current pulsar searching survey, 1200 is the minimum number of the dispersion trials. Based on the size of the input beam file, this de-dispersion step takes 1 to 13 hours to finish and generate up to 90GB of de-dispersion files. Furthermore, for binary pulsar searching, every de-dispersion file needs another step of processing named accelerate. This step generates the accelerated de-dispersion files with the similar size in the last de-dispersion step. Based on the generated de-dispersion files, different seeking algorithms can be applied to search pulsar candidates, such as FFT Seeking, FFA Seeking, and Single Pulse Seeking. For a large input beam file, it takes more than one hour to seek the 1200 de-dispersion files. A candidate list of pulsars is generated after the seeking step which is saved in a text file. Furthermore, by comparing the candidates generated from different beam files in a same time session, some interferences may be detected and some candidates may be eliminated. With the final pulsar candidates, we need to go back to the de-dispersion files to find their feature signals and fold them to XML files. At last, the XML files are visually displayed to scientists for making decisions on whether a pulsar has been found or not.
As described above, we can see that this pulsar searching workflow is both computation- and data-intensive. It needs long execution time and large datasets are generated. At present, all the generated datasets are deleted after having been used, and the scientists only store the raw beam data extracted from the raw telescope data. Whenever there are needs of using the deleted datasets, the scientists will regenerate them based on the raw beam files. The generated datasets are not stored, mainly because the supercomputer is a shared facility that cannot offer unlimited storage capacity to hold the accumulated terabytes of data. However, some datasets are better to be stored. For example, the de-dispersion files, which are frequently used. Based on them, the scientists can apply different seeking algorithms to find potential pulsar candidates. Furthermore, some datasets are derived from the de-dispersion files, such as the results of the seek algorithms and the pulsar candidate list. If these datasets need to be regenerated, the de-dispersion files will also be reused. For the large input beam files, the regeneration of the de-dispersion files will take more than 10 hours. It not only delays the scientists from conducting their experiments, but also requires a lot of computation resources. On the other hand, some datasets need not be stored. For example, the accelerated de-dispersion files, which are generated by the accelerate step. The accelerate step is an optional step that is only for the binary pulsar searching. Not all pulsar searching processes need to accelerate the de-dispersion files, so the accelerated de-dispersion files are not that often used. In light of this and given the large size of these datasets, they are not worth storing as it would be more cost effective to regenerate them from the de-dispersion files whenever used.

2.2 Problem analysis

Traditionally, scientific workflows are deployed on the high performance computing facilities, such as clusters and grids. Scientific workflows are often complex with huge intermediate datasets generated during their execution. How to store these intermediate datasets is normally decided by the scientists who use the scientific workflows. This is because the clusters and grids only serve for certain institutions. The scientists may store the intermediate datasets that are most valuable to them, based on the storage capacity of the system. However, in many scientific workflow systems, the storage capacities are limited, such as the pulsar searching workflow introduced above. The scientists have to delete all the intermediate datasets because of the storage limitation. This bottleneck of storage can be avoided if we run scientific workflows in the cloud.

In a cloud computing environment, theoretically, the system can offer unlimited storage resources. All the intermediate datasets generated by scientific cloud workflows can be stored, if we are willing to pay for the required resources. However, in scientific cloud workflow systems, whether to store intermediate datasets or not is not an easy decision anymore due to the reasons below.

1) All the resources in the cloud carry certain costs, so either storing or generating an intermediate dataset, we have to pay for the resources used. The intermediate datasets vary in size, and have different generation costs and usage rates. Some of them may be used frequently whilst some others may be not. On one hand, it is most likely not cost effective to store all the intermediate datasets in the cloud. On the other hand, if we delete them all, regeneration of frequently used intermediate datasets imposes a high computation cost. Different storage strategies can be applied to the scientific cloud workflow systems, and will lead to different costs. Traditionally, intermediate datasets storage strategies may be developed based on different factors, such as security, users’ preference etc., but in scientific cloud workflow systems, all the strategies should deem system cost as an important factor. Hence a benchmarking of the minimum system
cost is needed to evaluate the cost effectiveness of different intermediate datasets storage strategies.

2) The usages of intermediate datasets are dynamic. For a single research group, scientists can estimate the intermediate datasets’ usages, since they are the only users of the datasets. But for the datasets that are shared among different institutions, their usages are hard to predict. In cloud computing environment, the users could be anonymous from the Internet and a shared dataset may be used by many users. Hence the datasets’ usages are dynamic in scientific cloud workflow systems, and the minimum cost of the system is also a dynamic value. The minimum cost benchmarking should be based on the datasets’ usages that are determinate by all the cloud users, hence should be discovered and obtained from the system logs.

Hence, we need an algorithm to find the minimum cost storage strategy for the intermediate datasets in the scientific cloud workflow systems based on the historic usages of the datasets. This strategy can be used as a benchmark to evaluate the cost effectiveness over other intermediate datasets storage strategies.

3. Concepts and model of cost oriented intermediate datasets storage in scientific cloud workflows

In this section, based on our prior work [36] [38], we introduce some important concepts, and enhance the representation of IDG and the datasets storage cost model in scientific cloud workflow systems.

3.1 Classification of the application data in scientific cloud workflows

In general, there are two types of data stored in the cloud storage, input data and intermediate data (including result data).

First, input data are the data uploaded by users, and in scientific applications they also can be the raw data collected from the devices. These data are the original data for processing or analysis which are usually the input of the applications. The most important feature of these data is that if they are deleted, they cannot be regenerated by the system.

Second, intermediate data are the data newly generated in the cloud system while the applications run. These data save the intermediate computation results of the applications which will be used in future execution. In general, the final result data of the applications are a kind of intermediate data because the result data in one application can also be used in other applications. When further operations apply to the result data, they become intermediate data. Therefore, the intermediate data are the data generated by computations on either the input data or other intermediate data, and their most important feature is that they can be regenerated if we know their provenance.

For the input data, the users will decide whether they should be stored or deleted, since they cannot be regenerated once deleted. For the intermediate data, their storage status can be decided by the system, since they can be regenerated. Hence, our minimum cost storage strategy only applies to the intermediate data in the scientific cloud workflow systems. In this paper, we refer intermediate data as dataset(s).

3.2 Data provenance and Intermediate data Dependency Graph (IDG)

Scientific workflows have many computation and data intensive tasks that generate many intermediate datasets of considerable size. There exist dependencies among the intermediate datasets. Data provenance in workflows is a kind of important metadata in which the
dependencies between datasets are recorded [31]. The dependency depicts the derivation relationship between workflow intermediate datasets. For scientific workflows, data provenance is especially important because after the execution, some intermediate datasets may be deleted, but sometimes the scientists have to regenerate them for either reuse or reanalysis [13]. Data provenance records the information of how the intermediate datasets were generated, which is very important for the scientists. Furthermore, regeneration of the intermediate datasets from the input data may be very time consuming, and therefore carry a high cost. On the contrary, with data provenance information, the regeneration of the demanding dataset may start from some stored intermediated datasets. In the scientific cloud workflow system, data provenance is recorded along the workflow execution. Taking the advantage of data provenance, we can build IDG. All the intermediate datasets once generated (or modified) in the system, whether stored or especially important because after the execution, some intermediate datasets may be deleted, but dependencies between datasets are recorded [31]. The dependency depicts the derivation relationship between workflow intermediate datasets. For scientific workflows, data provenance is especially important because after the execution, some intermediate datasets may be deleted, but sometimes the scientists have to regenerate them for either reuse or reanalysis [13]. Data provenance records the information of how the intermediate datasets were generated, which is very important for the scientists. Furthermore, regeneration of the intermediate datasets from the input data may be very time consuming, and therefore carry a high cost. On the contrary, with data provenance information, the regeneration of the demanding dataset may start from some stored intermediated datasets. In the scientific cloud workflow system, data provenance is recorded along the workflow execution. Taking the advantage of data provenance, we can build IDG. All the intermediate datasets once generated (or modified) in the system, whether stored or deleted, their references are recorded in the IDG as different nodes.

![Figure 2. A simple Intermediate data Dependency Graph (IDG)](image)

In IDG, every node denotes an intermediate dataset. Figure 2 shows us a simple IDG, dataset $d_i$ pointing to $d_2$ means that $d_i$ is used to generate $d_2$; and $d_2$ pointing to $d_3$ and $d_5$ means that $d_2$ is used to generate $d_3$ and $d_5$ based on different operations; datasets $d_4$ and $d_6$ pointing to $d_7$ means that $d_4$ and $d_6$ are used together to generate $d_7$.

IDG is a directed acyclic graph (DAG), where no circles exist. This is because IDG records the provenances of how datasets are derived in the system as time goes on. In another word, it depicts the generation relationships of datasets.

When some of the deleted intermediate datasets need to be reused, we do not need to regenerate them from the original input data. With IDG, the system can find the predecessors of the demanding dataset, so they can be regenerated from their nearest stored predecessors.

We denote a dataset $d_i$ in IDG as $d_i \in IDG$, and a set of datasets $S=\{d_1, d_2 \ldots d_n\}$ in IDG as $S \subseteq IDG$. To better describe the relationships of datasets in IDG, we define two symbols, $\rightarrow$ and $\leftrightarrow$:

$\rightarrow$ denotes that two datasets have a generation relationship, where $d_i \rightarrow d_j$ means $d_i$ is a predecessor dataset of $d_j$ in IDG. For example, in Figure 2’s IDG, we have $d_1 \rightarrow d_2$, $d_1 \rightarrow d_4$, $d_5 \rightarrow d_7$, $d_1 \rightarrow d_7$, etc. Furthermore, $\rightarrow$ is transitive, where $d_i \rightarrow d_j \rightarrow d_k \iff d_i \rightarrow d_j \land d_j \rightarrow d_k \Rightarrow d_i \rightarrow d_k$.

$\leftrightarrow$ denotes that two datasets do not have a generation relationship, where $d_i \leftrightarrow d_j$ means $d_i$ and $d_j$ are in different branches in IDG. For example, in Figure 2’s IDG, we have $d_3 \leftrightarrow d_5$, $d_3 \leftrightarrow d_6$, etc. Furthermore, $\leftrightarrow$ is commutative, where $d_i \leftrightarrow d_j \iff d_j \leftrightarrow d_i$.

### 3.3 Datasets storage cost model

With IDG, given any intermediate datasets that ever existed in the system, we know how to regenerate it. In this paper, we aim at minimising the total cost of managing the intermediate datasets. In a cloud computing environment, if the users want to deploy and run applications, they need to pay for the resources used. The resources are offered by cloud service providers, who have their cost models to charge the users. In general, there are two basic types of resources in
cloud computing: storage and computation. Popular cloud services providers’ cost models are based on these two types of resources [1]. For example, Amazon cloud services’ prices are as follow:

- $0.15 per Gigabyte per month for the storage resources.
- $0.1 per CPU instance-hour for the computation resources.

Furthermore, the cost of data transfer is also considered, such as in Amazon clouds’ cost model. In [19], the authors state that a cost-effective way of doing science in the cloud is to upload all the application data to the cloud and run all the applications in the cloud services. So we assume that the scientists upload all the input data to the cloud to conduct their experiments. Because transferring data within one cloud service provider’s facilities is usually free, the data transfer cost of managing intermediate datasets during the workflow execution is not counted. In this paper, we define our cost model for managing the intermediate data in a scientific cloud workflow system as follows:

\[ \text{Cost} = C + S \]

where the total cost of the system, \( C \), is the sum of \( C \), which is the total cost of computation resources used to regenerate the intermediate datasets, and \( S \), which is the total cost of storage resources used to store the intermediate datasets.

To utilise the cost model, we define some important attributes for the intermediate datasets in IDG. For intermediate dataset \( d_i \), its attributes are denoted as: \( <x_i, y_i, f_i, t_i, provSet_i, CostR_i> \), where

- \( x_i \) denotes the generation cost of dataset \( d_i \) from its direct predecessors. To calculate this generation cost, we have to multiply the time of generating dataset \( d_i \) by the price of computation resources. Normally the generating time can be obtained from the system logs.
- \( y_i \) denotes the cost of storing dataset \( d_i \) in the system per time unit. This storage cost can be calculated by multiplying the size of dataset \( d_i \) and the price of storage resources.
- \( f_i \) is a flag, which denotes the status whether this dataset is stored or deleted in the system.
- \( t_i \) denotes the usage rate, which is the time between every usage of \( d_i \) in the system. In traditional scientific workflows, \( t_i \) can be defined by the scientists, who use this workflow collaboratively. However, a scientific cloud workflow system is based on the Internet with large number of users, as we discussed before, \( t_i \) cannot be defined by users. It is a forecasting value from the dataset’s usage history recorded in the system logs.

- \( provSet_i \) denotes the set of stored provenance datasets that are needed when regenerating dataset \( d_i \), in another word, it is the set of stored predecessor datasets that are adjacent to \( d_i \) in IDG. If we want to regenerate \( d_i \), we have to find its direct predecessors, which may also be deleted, so we have to further find the stored predecessors of datasets \( d_i \). \( provSet_i \) is the set of the nearest stored predecessors of \( d_i \) in IDG. Figure 3 shows the \( provSet \) of a dataset in different situations.
Formally, we can describe a dataset \( d_i \)'s ProvSet, as follows:

\[
\text{ProvSet} = \{ d_i \mid d_i \in \text{IDG} \land f_j = \text{"stored"} \land d_j \rightarrow d_i \\
\land \left( \neg \exists d_k \in \text{IDG} \land d_j \rightarrow d_k \rightarrow d_i \right) \lor \left( \exists d_k \in \text{IDG} \land d_j \rightarrow d_k \rightarrow d_i \land f_k = \text{"deleted"} \right) \} \]

\( \text{provSet} \) is a very important attribute of a dataset in calculating its generation cost. When we want to regenerate a dataset in IDG, we have to start the computation from the dataset in its provSet. Hence, for dataset \( d_i \), its generation cost is:

\[
\text{genCost}(d_i) = x_i + \sum_{d_j \in \text{provSet}_i, d_j \rightarrow d_i} x_k
\]  

(1)

This cost is a total cost of 1) the generation cost of dataset \( d_i \) from its direct predecessor datasets and 2) the generation costs of \( d_i \)'s deleted predecessors that need to be regenerated.

\( \text{CostR}_i \) is \( d_i \)'s cost rate, which means the average cost per time unit of the dataset \( d_i \) in the system. If \( d_i \) is a stored dataset, then \( \text{CostR}_i = y_i \). If \( d_i \) is a deleted dataset in the system, when we need to use \( d_i \), we have to regenerate it. So we divide the generation cost of \( d_i \) by the time between its usages and use this value as the cost rate of \( d_i \) in the system. \( \text{CostR}_i = \text{genCost}(d_i)/t_i \).

The storage statuses of the datasets have strong impact on their cost rates. If \( d_i \)'s storage status is changed, not only the cost rate of itself, \( \text{CostR}_i \), will change, but also the generation cost of \( d_i \)'s successors will change correspondingly.

Hence, the system cost rate of managing intermediate datasets is the sum of \( \text{CostR} \) of all the intermediate datasets, which is \( \sum_{d_i \in \text{IDG}} \text{CostR}_i \). We further define the storage strategy of an IDG as \( S \), where \( S \subseteq \text{IDG} \), which means storing the datasets in \( S \) in the cloud and deleting the others. We denote the cost rate of storing an IDG with the storage strategy \( S \) as \( \left\{ \sum_{d_i \in \text{IDG}} \text{CostR}_i \right\}_S \). Given a time duration, denoted as \([T_0, T_n]\), the total system cost is the integral of the system cost rate in this duration as a function of time \( t \), which is:

\[
\text{Total Cost} = \int_{T_0}^{T_n} \left( \sum_{d_i \in \text{IDG}} \text{CostR}_i \right) dt \]

(2)

Based on the definition of the dataset’s cost rate, the system’s cost rate highly depends on the storage strategy of the intermediate datasets. Storing different intermediate datasets will lead to different cost rates of the system. In scientific cloud workflow systems, intermediate datasets storage strategies should try to reduce this cost rate.

### 4. Minimum cost benchmarking of intermediate datasets storage

The cost rate of scientific applications in the cloud is dynamic. Based on the cost model discussed in Section 3, in scientific cloud workflow systems, the system cost rate may differ a lot with different intermediate datasets storage strategies. However, based on datasets’ usage rates derived from system logs at the time, there exists a minimum cost rate of storing them, which can be used for on-demand benchmarking. In this section, we describe the design of a Cost Transitive Tournament Shortest Path (CTT-SP) based algorithm that can find the minimum cost storage strategy for a given IDG. The basic idea of the CTT-SP algorithm is to construct a Cost Transitive Tournament (CTT) based on the IDG. In a CTT, we guarantee that the paths from the start dataset to the end dataset have a one-to-one mapping to the storage strategies, and the length of every path equals the total cost rate. Then we can use the well known Dijkstra algorithm to find the shortest path in the CTT, which is also the minimum cost storage strategy. To describe the algorithm, we start with calculation of the minimum cost benchmark for the linear IDG, and then expand it to the general complex IDG, followed by algorithm complexity analysis.
4.1 Minimum cost algorithm for linear IDG

Linear IDG means an IDG with no branches, where each dataset in the IDG only has one direct predecessor and successor except the first and last datasets.

Given a linear IDG, which has datasets \( d_1, d_2 \ldots d_n \), The CTT-SP algorithm has the following four steps:

**Step 1:** We add two virtual datasets in the IDG, \( d_i \) before \( d_j \) and \( d_e \) after \( d_n \), as the start and end datasets, and set \( x_i = y_i = 0 \) and \( x_e = y_e = 0 \).

**Step 2:** We add new directed edges in the IDG to construct the transitive tournament. For every dataset in the IDG, we add edges that start from it and point to all its successors. Formally, for dataset \( d_n \) it has out-edges to all the datasets in the set of \( \{ d_j | d_j \in IDG \wedge d_j \to d_n \} \), and in-edges from all the datasets in the set of \( \{ d_e | d_e \in IDG \wedge d_e \to d_n \} \). Hence, for any two datasets \( d_i \) and \( d_j \) in the IDG, we have an edge between them, denoted as \( e < d_i, d_j > \). Formally, \( d_i, d_j \in IDG \wedge d_i \to d_j \Rightarrow \exists e < d_i, d_j > \).

**Step 3:** We set weights to the edges. The reason we call the graph Cost Transitive Tournament is because the weights of its edges are composed of the cost rates of datasets. For an edge \( e < d_i, d_j > \), we denote its weight as \( \omega < d_i, d_j > \), which is defined as the sum of cost rates of \( d_j \) and the datasets between \( d_i \) and \( d_j \) supposing that only \( d_i \) and \( d_j \) are stored and rest of the datasets between \( d_i \) and \( d_j \) are all deleted. Formally:

\[
\omega < d_i, d_j > = y_j + \sum_{d_l \in IDG \wedge d_l \to d_j \wedge \neg d_l \to d_i} \left( \text{genCost}(d_l) / t_l \right)
\]

Since we are discussing the linear IDG, for the datasets between \( d_i \) and \( d_j \), \( d_i \) is the only dataset in their provSets. Hence we can further get:

\[
\omega < d_i, d_j > = y_j + \sum_{d_l \in IDG \wedge d_l \to d_j \wedge \neg d_l \to d_i} \left( x_k + \sum_{d_l \in IDG \wedge d_l \to d_j \wedge \neg d_l \to d_i} x_l \right) / t_l
\]

In Figure 4, we demonstrate a simple example of constructing CTT for an IDG that only has three datasets, where \( d_s \) is the start dataset that only has out-edges and \( d_e \) is the end dataset that only has in-edges.

![Figure 4. An example of constructing CTT](image)

**Step 4:** We find the shortest path of CTT. From the construction steps, we can clearly see that the CTT is an acyclic complete oriented graph. Hence we can use the Dijkstra algorithm to find the shortest path from \( d_s \) to \( d_e \). The Dijkstra algorithm is a classic greedy algorithm to find the shortest path in graph theory. We denote the shortest path from \( d_s \) to \( d_e \) as \( P_{\text{min}<d_s, d_e>} \).
**Theorem 1:** Given a linear IDG with datasets \( \{d_1, d_2 \ldots d_n\} \), the length of \( P_{min}(d_i, d_e) \) of its CTT is the minimum cost rate of the system to store the datasets in the IDG, and the corresponding storage strategy is to store the datasets that \( P_{min}(d_i, d_e) \) traverses.

**Proof:**
First, there is a one-to-one mapping between the storage strategies of the IDG and the paths from \( d_i \) to \( d_e \) in the CTT. Given any storage strategy of the IDG, we can find an order of these stored datasets, since the IDG is linear. Then we can find the exact path in the CTT that has traversed all these stored datasets. Similarly, given any path from \( d_i \) to \( d_e \) in the CTT, we can find the datasets it has traversed, which is a storage strategy. Second, based on the setting of weights to the edges, the length of a path from \( d_i \) to \( d_e \) in the CTT equals to the total cost rate of the corresponding storage strategy. Third, \( P_{min}(d_i, d_e) \) is the shortest path from \( d_i \) to \( d_e \) as found by the Dijkstra algorithm. **Hence, Theorem 1 holds.**

**Corollary 1:** During the process of finding the shortest path, for every dataset \( d_j \) that is discovered by the Dijkstra algorithm, we have a path \( P_{min}(d_i, d_j) \) from \( d_i \) to \( d_j \) and a set of datasets \( S_j \) that \( P_{min}(d_i, d_j) \) traverses. \( S_j \) is the minimum cost storage strategy of the sub-IDG \( \{d, d_j \in \text{IDG} \land d_i \rightarrow d_j \rightarrow d_e\} \). Then we can get a path \( P_{min}(d_i, d_j) \) from \( d_i \) to \( d_j \), which traverses the datasets in \( S_j \). Then we have:

\[
P_{min}(d_i, d_j) = \left\{ \sum_{d \in \text{IDG} \land d_i \rightarrow d} \text{CostR} \right\}_{S_j} < \left\{ \sum_{d \in \text{IDG} \land d_i \rightarrow d} \text{CostR} \right\}_{S_j} = P_{min}(d_i, d_j)
\]

This is contradictory to the known condition "\( P_{min}(d_i, d_j) \) is the shortest path from \( d_i \) to \( d_j \)." Hence, \( S_j \) is the minimum cost storage strategy of the sub-IDG \( \{d, d_j \in \text{IDG} \land d_i \rightarrow d_i \rightarrow d_j\} \). **Hence, Corollary 1 holds.**

<table>
<thead>
<tr>
<th>Algorithm:</th>
<th>Linear_CTT-SP</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Input:</strong></td>
<td>start dataset ( d_i ) end dataset ( d_e ); a linear IDG; ( d_i ) and ( d_e ); a set of datasets in IDG ( d_i ) and ( d_e ); ( S_i ) is the minimum cost storage strategy</td>
</tr>
<tr>
<td><strong>Output:</strong></td>
<td></td>
</tr>
</tbody>
</table>

01. For \( (\text{every dataset } d_i \text{ in IDG}) \) //Create CTT
02. For \( (\text{every dataset } d_i \text{ where } d_i \rightarrow d_j) \)
03. \( e \leftarrow d_i, d_j \) //Create an edge
04. \( \text{weight} = 0 \)
05. For \( (\text{every dataset } d_h \text{ where } d_i \rightarrow d_h \rightarrow d_j) \) //Calculate the weight of an edge
06. \( \text{genCost} = 0 \)
07. \( \{ \)
08. \( \{ \text{For (every dataset } d_h \text{ where } d_i \rightarrow d_h \rightarrow d_j) \) \)
09. \( \text{genCost} = \text{genCost} + x_h; \)
10. \( \text{weight} = \text{weight} + (x_h + \text{genCost})/t_h; \) //Accumulate generation cost rate
11. \( \text{Set } \omega \leftarrow d_i, d_j \rightarrow \text{weight}; \) //Set weight to an edge
12. \( P_{min}(d_i, d_j) = \text{Dijkstra Algorithm (} d_i, d_e, \text{CTT)} \) //Find the shortest path
13. \( S \leftarrow \text{set of datasets that } P_{min}(d_i, d_j) \text{ traversed}; \) //Except \( d_i \) and \( d_e \)
14. Return \( S \)

**Figure 5. Pseudo-code of linear CTT-SP algorithm**
Figure 5 shows the pseudo-code of the linear CTT-SP algorithm. To construct the CTT, we first create the cost edges (line 3), and then calculate their weights (lines 4 to 11). Next, we use the Dijkstra algorithm to find the shortest path (line 12), and return the minimum cost storage strategy (lines 13 to 14).

4.2 Minimum cost algorithm for IDG with one block

Linear IDG is a special case of general IDGs. In the real world, intermediate datasets generated in scientific workflows may have complex relationships, such that different datasets may be generated from a single dataset by different operations, and different datasets may be used together to generate one dataset. In another word, the IDG may have branches, where the linear CTT-SP algorithm introduced in Section 4.1 cannot be directly applied. This is because the CTT can only be constructed on linear IDG, which means the datasets in the IDG must be totally ordered. In this section, we discuss how to find the minimum cost storage strategy for the IDG that has a sub-branch within one block.

4.2.1 Construct CTT for IDG with a block

First we introduce a concept of “block” in IDG. Block is a set of sub-branches in the IDG that split from a common dataset and merge into another common dataset. We denote the block as B. Figure 6 shows an IDG with a simple block $B=\{d_3, d_4, d_5, d_6\}$, we will use it as the example to illustrate the construction of CTT.

To construct the CTT, we need the datasets in IDG to be totally ordered. Hence, for the IDG with a block, we only choose one branch to construct the CTT, as shown is Figure 6. We call the linear datasets which are chosen to construct the CTT “main branch”, denoted as $MB$, and call the rest of the datasets “sub-branches”, denoted as $SB$. For example, in Figure 6’s IDG, $MB=\{d_1, d_2, d_5, d_6, d_7, d_8\}$ and $SB=\{d_3, d_4\}$. Due to the existence of the block, the edges can be classified into four categories. The definition of this classification is as follows:
• **in-block edge:** $e<d_i, d_j>$ is an in-block edge meaning that the edge starts from $d_i$, which is a dataset outside of the block, and points to $d_j$, which is a dataset in the block, such as $e<d_2, d_5>$, $e<d_1, d_6>$ in Figure 6. Formally, we define $e<d_i, d_j>$ as an in-block edge, where $\exists d_k \in IDG \land d_i \rightarrow d_k \land d_k \leftrightarrow d_j$.

• **out-block edge:** $e<d_i, d_j>$ is an out-block edge meaning that the edge starts from $d_i$, which is a dataset in the block, and points to $d_j$, which is a dataset outside of the block, such as $e<d_6, d_7>$, $e<d_5, d_8>$ in Figure 6. Formally, we define $e<d_i, d_j>$ as an out-block edge, where $\exists d_k \in IDG \land d_i \leftrightarrow d_k \land d_k \rightarrow d_j$.

• **over-block edge:** $e<d_i, d_j>$ is an over-block edge meaning that the edge crosses over the block, where $d_i$ is a dataset preceding the block, $d_j$ is a dataset succeeding the block, such as $e<d_2, d_3>$, $e<d_1, d_5>$ in Figure 6. Formally, we define $e<d_i, d_j>$ as an over-block edge, where $\exists d_k \in IDG \land d_i \leftrightarrow d_k \land d_k \rightarrow d_j \land d_j \rightarrow d_k \land d_k \rightarrow d_j$.

• **ordinary edge:** $e<d_i, d_j>$ is an ordinary edge meaning that datasets between $d_i$ and $d_j$ are totally ordered, such as $e<d_1, d_2>$, $e<d_3, d_4>$, $e<d_7, d_8>$ in Figure 6. Formally, we define $e<d_i, d_j>$ as an ordinary edge, where $\neg \exists d_k \in IDG \land (d_i \rightarrow d_k \land d_k \leftrightarrow d_j) \lor (d_j \rightarrow d_k \land d_i \rightarrow d_j)$.

$\forall (d_i \in IDG \land d_i \leftrightarrow d_k \land d_k \rightarrow d_j \land d_j \rightarrow d_k \land d_k \rightarrow d_j)$

### 4.2.2 Setting weights to different types of edges

The essence of the CTT-SP algorithm is the rules of setting weights to the cost edges. Based on the setting, we guarantee that the paths from the start dataset $d_s$ to every dataset $d_i$ in the IDG represent the storage strategies of the datasets \( \{d_i \mid d_i \in IDG \land d_i \rightarrow d_s \} \), and the shortest path is the minimum cost storage strategy. As defined in Section 4.1, the weight of the edge $e<d_i, d_j>$ is the sum of cost rates of $d_i$ and the datasets between $d_i$ and $d_j$, supposing that only $d_i$ and $d_j$ are stored and the rest of the datasets between $d_i$ and $d_j$ are all deleted. In the IDG with one block, this rule is still applicable to the ordinary edges and in-block edges.

However, if $e<d_i, d_j>$ is an out-block edge or over-block edge, formula (3) in Section 4.1 is not applicable for calculating its weight anymore, because of the following reasons.

1) Due to the existence of the block, the datasets succeeding the block may have more than one datasets in their provSets. The generation of these datasets needs not only $d_i$, but also the stored provenance datasets from the other sub-branches of the block. For example, according to formula (3) in Section 4.1, the weight of the out-block edge $e<d_3, d_8>$ in Figure 6 is $\omega<d_3, d_8> \Rightarrow \gamma_i + \text{genCost}(d_3)\gamma_k + \text{genCost}(d_8)\gamma_j$, where if we want to calculate genCost($d_7$), we also have to know the storage statuses of $d_3$ and $d_8$. The same problem also exists when calculating the weights of the over-block edges. Hence, to calculate the weights of out-block and over-block edges, we have to know the storage strategies of all the sub-branches in the block.

2) The path from $d_1$ to $d_8$ cannot represent the storage strategy of all the datasets \( \{d_i \mid d_i \in IDG \land d_1 \rightarrow d_i \} \). If we use the same method in Section 4.1 to set the weight of $e<d_i, d_j>$, the path that contains $e<d_i, d_j>$ in the CTT can only represent the storage strategy of datasets in the main branch, where the sub-branches are not represented. For example, in Figure 6, the path from $d_1$ to $d_8$ that contains the out-block edge $e<d_5, d_8>$, does not represent the storage statuses of datasets $d_5$ and $d_8$ and the length of the path also does not contain the cost rates of $d_5$ and $d_8$, if we use the method in Section 4.1 to calculate the weights of the edges. Hence, to maintain the mapping between the paths and the storage strategies, the weights of out-block and
over-block edges should contain the minimum cost rates of the datasets in the sub-branches of the block.

Based on the reasons above, we define the weight of $e<d_i, d_j>$ as

$$\omega < d_i, d_j >= y_j + \sum_{d_k \in MB \cap d_i \rightarrow d_k \rightarrow d_j} \left( \frac{genCost(d_k)}{t_k} \right) + \left( \frac{d_j}{SB} \cdot CostR_j \right)_{s_{min}}$$

(5)

In formula (5), $\left( \frac{d_j}{SB} \cdot CostR_j \right)_{s_{min}}$ means the minimum cost rates of the datasets that are in the sub-branches of the block. This formula guarantees that the length of the shortest path with an out-block edge or over-block edge still equals the minimum cost rate of the datasets, which is $P_{s_{min}} < d_i, d_j >= \left( \sum_{d_k \in IDG, d_i \rightarrow d_k \rightarrow d_j} \cdot CostR \right)_{s_{min}}$. Hence, to calculate the weights of out-block and over-block edges, we have to find the minimum cost storage strategy of the datasets that are in the sub-branches of the block. For example, the weight of the edge $e<d_s, d_g>$ in Figure 6 is $\omega < d_s, d_g >= y_g + genCost(d_g)/t_g + genCost(d_t)/t_t + (CostR_s + CostR_t)_{s_{min}}$, where we have to find the minimum cost storage strategy of datasets $d_3$ and $d_4$.

However, for any sub-branches, the minimum cost storage strategy is dependant on the storage status of the datasets preceding and succeeding the block (i.e. stored adjacent predecessor and successor of the sub-branches).

If $e<d_i, d_j>$ is an over-block edge, according to its semantics, $d_i$ and $d_j$ are stored datasets, and the datasets between $d_i$ and $d_j$ in the main branch, $\{ d_k \in MB \cap d_i \rightarrow d_k \rightarrow d_j \}$, are deleted. Hence, $d_i$ and $d_j$ are the stored adjacent predecessor and successor of the sub-branches. If the rest datasets within the block form a linear IDG, we can use the linear CTT-SP algorithm introduced in Section 4.1 to find its minimum cost storage strategy, where in the first step we have to use $d_i$ and $d_j$ as the start and end datasets. For example, to calculate the weight of over-block edge $e<d_i, d_g>$ in Figure 6, we have to find the minimum cost storage strategy of sub-branch $\{ d_t, d_g \}$ by the linear CTT-SP algorithm, given, $d_i$ is the start dataset and $d_g$ is the end dataset. Otherwise, if the rest datasets within the block do not form a linear IDG, we have to recursively call the CTT-SP algorithm to find the minimum cost storage strategy of sub-branches, which will be introduced in Section 4.3. Hence, the weight of an over-block edge can be calculated.

If $e<d_i, d_j>$ is an out-block edge, we only know the stored adjacent successor of the sub-branches is $d_j$. However, the minimum cost storage strategy of the sub-branches is also dependant on the stored adjacent predecessor, which is unknown for an out-block edge. Hence, given different stored adjacent predecessors, the weight of an out-block edge would be different. For example, to calculate the weight of out-block edge $e<d_s, d_g>$ in Figure 6, we need to find the minimum cost storage strategy $S_{s_{min}}$ of the sub-branch $\{ d_s, d_g \}$, where we only know the stored adjacent successor $d_g$. However, $S_{s_{min}}$ may be different depending on the storage statuses of $d_i$ and $d_2$. Hence, we have to create multiple CTTs for the IDG that has a block, in order to calculate the weights of out-block edges in different situations, as detailed next.

4.2.3 Steps of finding minimum cost storage strategy for IDG with one sub-branch in block

In this section, we extend the linear CTT-SP algorithm to find its minimum cost storage strategy for IDG with one sub-branch in block. As discussed in Section 4.2.2, depending on different stored preceding datasets of the block, the weight of an out-block edge may be different. Hence multiple CTTs are needed to represent these different situations, and the minimum cost storage strategy is the shortest path among all the CTTs.

For developing the minimum cost storage strategy, we need the following two theorems.
**Theorem 2:** The selection of main branch in the IDG to construct CTT has no impact on finding the minimum cost storage strategy.

**Proof:**

Assume that strategy $S$ is the minimum cost storage strategy of an IDG; the IDG has two sub-branches $Br_1$ and $Br_2$ in a block; strategies $S_1$ and $S_2$ contain the sets of stored datasets of $Br_1$ and $Br_2$ in $S$.

If we select the main branch with the sub-branch $Br_1$, $S$ can be mapped to a path in one of the created CTTs. According to Theorem 1, the paths in CTT have one-to-one mapping to the storage strategies, hence we can find a path $P<d_i, d_e>$ that traverses the stored datasets in the main branch according to $S$. If $S_1 = \emptyset$, there is an over-block edge in the path $P<d_i, d_e>$, which contains the minimum cost storage strategy of $Br_2$ according to formula (5), where $P<d_i, d_e>$ is in the initial CTT. If $S_1 \neq \emptyset$, there is an in-block edge and an out-block edge in $P<d_i, d_e>$, denoted as $e<d_i, d>$ and $e<d_h, d_i>$. The weight of $e<d_h, d_i>$ contains the minimum cost storage strategy of $Br_2$ according to formula (5), hence $P<d_i, d_e>$ is in CTT($e<d_i, d_e>$). Similar to Theorem 1, we can further prove that the length of $P<d_i, d_e>$ equals the total cost rate of the storage strategy $S$.

Similarly, if we select the main branch with the sub-branch $Br_2$, $S$ can also be mapped to a path in one of the created CTTs, where the length of the path equals to the total cost rate of the minimum cost storage strategy.

Therefore, no matter which branch we select as main branch to construct CTT, the minimum cost storage strategy always exists in one of the created CTTs. This means that the selection of main branch has no impact on finding the minimum cost storage strategy. **Hence, Theorem 2 holds.**

**Theorem 3:** The Dijkstra algorithm is still applicable to find the minimum cost storage strategy of the IDG with one block.

**Proof:**

In the CTTs created for the IDG with one block, every path from $d_s$ to $d_e$ contains an out-block edge or over-block edge. According to formula (5), the minimum cost rate of the sub-branch is contained in the weights of out-block and over-block edges. Hence, every path from $d_s$ to $d_e$ in the CTT contains the minimum cost storage strategy of the sub-branch. Furthermore, the CTTs are created based on the main branch of the IDG, similar to the proof of Theorem 1, the shortest path $P_{min}<d_s, d_e>$ found by the Dijkstra algorithm contains the minimum cost storage strategy of the main branch. This means that $P_{min}<d_s, d_e>$ represents the minimum cost storage strategy of the whole IDG. **Hence, Theorem 3 holds.**

The main steps of the algorithm are as follows.

**Step 1:** Construct the initial CTT of the IDG. According to Theorem 2, we choose an arbitrary branch in the IDG as the main branch and add cost edges to construct the CTT. In the CTT, for the ordinary edges and in-block edges, we set their weights based on formula (3) in Section 4.1. For the over-block edges, we set their weights according to formula (5) by calling the linear CTT-SP algorithm to find the minimum cost storage strategy of the sub-branch, which is introduced in Section 4.2.2. For the out-block edges, we set their weights as infinity at the initial stage. The initial CTT is shown in Figure 7 (a).

**Step 2:** Based on Theorem 3, start the Dijkstra algorithm to find the shortest path from $d_s$ to $d_e$. We use $F$ to denote the set of datasets discovered by the Dijkstra algorithm. When a new edge $e<d_i, d>$ is discovered, we first add $d_i$ to $F$, and then check whether $e<d_i, d>$ is an in-block edge...
or not. If not, we continue to find the next edge by the Dijkstra algorithm until $d_e$ is reached which would terminate the algorithm. If $e<d_i, d_j>$ is an in-block edge, create a new CTT (see steps 2.1 - 2.3 next) because whenever an in-block edge is discovered, a stored adjacent predecessor of the sub-branch is identified, and this dataset will be used in calculating the weights of out-block edges.

**Step 2.1:** In the case where in-block edge $e<d_i, d_j>$ is discovered, based on the current CTT, create CTT($e<d_i, d_j>$) as shown in Figure 7 (b). First, we copy all the information of the current CTT to the new CTT($e<d_i, d_j>$). Second, we update the weights of all the in-block edges in CTT($e<d_i, d_j>$) as infinity, except $e<d_i, d_j>$. This guarantees that dataset $d_i$ is the stored adjacent predecessor of the sub-branch in all the paths of CTT($e<d_i, d_j>$). Third, we update the weights of all the out-block edges in CTT($e<d_i, d_j>$) as described in Step 4 next.

**Step 2.2:** Calculate the weight of an out-block edge $e<d_h, d_k>$ in CTT($e<d_i, d_j>$). As discussed in Section 4.2.2, to calculate the weight of $e<d_h, d_k>$ according formula (5), we have to find the minimum cost storage strategy of the sub-branch in the block. From Figure 7 (b) we can see that the sub-branch is \{d'_1, d'_2, \ldots, d'_m\}, which is a linear IDG. We can find its minimum cost storage strategy by using the linear CTT-SP algorithm described in Section 4.1, given that $d_i$ is the start dataset and $d_k$ is the end dataset. The CTT created for the sub-branch is depicted in Figure 7 (c).

**Step 2.3:** Add the new CTT($e<d_i, d_j>$) to the CTTs set.

Figure 7. CTTs for the IDG with one block
4.3 Minimum cost algorithm for general IDG

In the real world applications, the structure of IDG could be complex, i.e. there may exist more than one block in an IDG. However, to calculate the minimum cost storage strategy of a general IDG, no matter how complex the IDG’s structure is, we can reduce the calculation process to the linear IDG situations by recursively calling the algorithm introduced in Section 4.2. In this section we introduce the general CTT-SP algorithm as well as the pseudo-code of calculating the minimum cost storage strategy for general IDG.

4.3.1 General CTT-SP algorithm

The complex structure of an IDG can be viewed as a combination of many blocks. Following the algorithm steps introduced in Section 4.2, we choose an arbitrary branch from the start dataset \(d_e\) to the end dataset \(d_d\) as the main branch to construct the initial CTT and create multiple CTTs for different in-block edges which are discovered by the Dijkstra algorithm. In the process of calculating the weights of out-block and over-block edges, there are two new situations of finding the minimum cost storage strategy of the sub-branches.

1) The sub-branches may have more than one stored adjacent predecessors. For example, \(e<d_i, d>\) in Figure 8 is an out-block edge of block \(B_1\), and also an in-block edge of block \(B_2\). In the algorithm, if edge \(e<d_i, d>\) is found by the Dijkstra algorithm, we create a new CTT(\(e<d_i, d>\)) from the current CTT, since \(e<d_i, d>\) is an in-block edge of block \(B_2\). To calculate the weights of out-block edges in CTT(\(e<d_i, d>\)), for example \(e<d_i, d>\) in Figure 8, we need to find the minimum cost storage strategy of the sub-branch \(
\{d_i', d_i'', \ldots, d_i''\}\) of block \(B_2\). However, because \(e<d_i, d>\) is also an out-block edge of \(B_1\), \(d_i\) is not the only dataset in \(d_i'\)’s provSet. To calculate the generation cost of \(d_i'\), we need to find its stored provenance datasets from the sub-branch \(Br_1\) of block \(B_1\).

![Figure 8. Sub-branch IDG has more than one stored adjacent predecessors](image)

2) The sub-branches are a general IDG which also has branches. In this situation, we need to recursively call the general CTT-SP algorithm to calculate its minimum cost storage strategy. For example, \(e<d_i, d>\) in Figure 9 is an in-block edge of blocks \(B_1\) and \(B_2\). If \(e<d_i, d>\) is selected by the algorithm, we need to create a new CTT(\(e<d_i, d>\)). To calculate the weight of \(e<d_i, d>\) in Figure 9, which is an out-block edge of both \(B_1\) and \(B_2\), we need to calculate the minimum cost storage strategy of the sub-branches \(Br_1\) and \(Br_2\). Hence we have to recursively call the general CTT-SP algorithm for the IDG \(Br_1 \cup Br_2\) , given the start dataset \(d_i\) and the end dataset \(d_k\).
Hence, given a general IDG, its structure can be viewed as the combination of many blocks. By recursively calling the general CTT-SP algorithm for the sub-branches, we can eventually find the minimum cost storage strategy of the whole IDG. Figure 10 shows an example of general IDG. To create CTT($e<d_i, d_o>$), we need to calculate the weights of all the out-block edges. For example, for an out-block edge $e<d_h, d_k>$, we need to further calculate the minimum cost storage strategy of the sub-branches $\{d_e \mid d_e \in IDG \land d_e \rightarrow d_i \land d_e \leftrightarrow d_j \land d_e \leftrightarrow d_k\}$, as shadowed in Figure 10, given the start dataset $d_i$ and the end dataset $d_o$.

Figure 9. Sub-branch IDG also has branches

Figure 10. CTT for general IDG

4.3.2 Pseudo-code of general CTT-SP algorithm

Figure 11 shows the pseudo-code of the general CTT-SP algorithm. At the beginning, we choose an arbitrary branch from $d_i$ to $d_o$ as the main branch to construct the initial CTT (lines 1 to 21), where we need to recursively call the general CTT-SP algorithm in calculating the weights for over-block edges (lines 11 to 14). Then we start the Dijkstra algorithm (lines 22 to 50). Whenever an in-block edge is found, we construct a new CTT with the following steps. First we create a copy of the current CTT, in which the in-block edge is found (line 31). Next, we update the weights of edges: lines 32 to 34 are for updating the weights of in-block edges and lines 35 to 49 are for updating the weights of out-block edges. If the sub-branch is a linear IDG, we call the linear CTT-SP algorithm described in Figure 5, otherwise we recursively call the general CTT-SP algorithm (lines 39 to 42). At last, we add the new CTT to the CTTSet (line 50) and continue the Dijkstra algorithm to find the next edge. When the end dataset $d_o$ is reached, the algorithm ends with the minimum cost storage strategy returned.
Algorithm: General_CTT-SP

Input: start dataset $d_i$; end dataset $d_j$; a general IDG; //Include $d_i$ and $d_j$
Output: a set of CTTs in the IDG; //The minimum cost storage strategy

01. Get a main branch $MB$ from IDG;
02. For (every dataset $d_i$ in $MB$) //Create initial CTT
03. For (every dataset $d_j$, where $d_j \in MB \land d_i \rightarrow d_j$)
04. Create $e < d_i, d_j >$; //Create an edge
05. If ( $\exists d_k \in IDG \land d_i \leftrightarrow d_k \land d_k < d_j$) //is an out-block edge
06. Set $\omega < d_i, d_j > := \infty$; //Calculate the weight of the edge
07. else
08. weight = 0;
09. If ( $\exists d_k \in MB \land d_i \rightarrow d_k \rightarrow d_j$) //is an over-block edge
10. $SB = \{d_k \in MB \land d_i \rightarrow d_k \rightarrow d_j\}$; //Get the sub-branches $SB$
11. If (SB is linear) //Find the minimum cost storage strategy of $SB$
12. $S' = $ General_CTT-SP($d_i, d_j, SB$);
13. else
14. $S' = $ General_CTT-SP($d_i, d_j, SB$);
15. weight = weight $+$ $\sum_{e \in SB} CostR_{e}$;
16. For (every dataset $d_k$, where $d_k \in MB \land d_i \rightarrow d_k \rightarrow d_j$) //Datasets in the main branch
17. genCost = 0;
18. For (every dataset $d_k$, where $d_k \in MB \land d_i \rightarrow d_k \rightarrow d_j$)
19. genCost = genCost $+$ $x_k$;
20. weight = weight $+$ $(x_k + genCost)/t_k$; //Sum of generation cost rates
21. Set $\omega < d_i, d_j > := weight + y_k$; //Set weight to the edge
22. CTTSet = $\{CTT_{in}\}$; //Set of all the created CTTs
23. $F = \{0\}$; //Set of datasets discovered by Dijkstra algorithm
24. While ( $d_i$ is not in $F$ )
25. For (every CTT in CTTSet) //Find the next edge for the shortest path
26. Find the next edge by Dijkstra algorithm;
27. Get the current shortest path in all the CTTs, which is with the edge $e < d_i, d_j > \epsilon CTT'$
28. Add $d_j$ to $F$;
29. If ( $\exists d_k \in IDG \land d_i \rightarrow d_k \rightarrow d_j$) //is an in-block edge
30. $BSet = \{B_k \in IDG \land d_i \epsilon B_k \land d_k \epsilon B_k\}$; //The blocks that contains $d_i$ but not $d_j$
31. Create a copy of CTT denoted as CTT($e = d_i, d_j$); //Create a new CTT for the in-block edge
32. For (every $B_k$ in $BSet$) //Update the weights of the in-blocks edges
33. For (every $e < d_i, d_j > \epsilon < d_i, d_j >$ where $d_i \not\epsilon B_k \land d_i \epsilon B_k$)
34. Set $\omega < d_i, d_j > := \infty$;
35. For (every $B_k$ in $BSet$) //Update the weights of the out-block edges
36. For (every $e < d_i, d_j >$ where $d_k \epsilon B_k \land d_i \rightarrow d_k \rightarrow d_j$)
37. weight = 0;
38. $SB = \{d_k \epsilon IDG \land d_i \rightarrow d_k \rightarrow d_j \land d_k \leftrightarrow d_j \land d_i \not\epsilon B_k\}$; //Get the sub-branches $SB$
39. If (SB is linear) //Find the minimum cost storage strategy of $SB$
40. $S' = $ Linear_CTT-SP($d_i, d_j, SB$);
41. else
42. $S' = $ General_CTT-SP($d_i, d_j, SB$);
43. weight = weight $+$ $\sum_{e \in SB} CostR_{e}$;
44. For (every dataset $d_k$, where $d_k \in MB \land d_i \rightarrow d_k \rightarrow d_j$) //Datasets in the main branch
45. genCost = 0;
46. For (every dataset $d_k$, where $d_k \in MB \land d_i \rightarrow d_k \rightarrow d_j$)
47. genCost = genCost $+$ $x_k$;
48. weight = weight $+$ $(x_k + genCost)/t_k$; //Sum of generation cost rates
49. Set $\omega < d_i, d_j > := weight + y_i$; //Set weight to the out-block edge
50. Add CTT($e = d_i, d_j$) to CTTSet;
51. Return $S$ = set of datasets that the shortest path from $d_i$ to $d_j$ has traversed;

Figure 11. Pseudo-code of general CTT-SP algorithm
4.4 Complexity analysis of minimum cost algorithms

From the pseudo-code in Figure 5, we can clearly see that for a linear IDG with \( n \) datasets, we have to add a magnitude of \( n^2 \) edges to construct the CTT (line 3 with two nested loops in lines 1 to 2), and for the longest edge, the time complexity of calculating its weight is also \( O(n^2) \) (lines 5 to 11 with two nested loops), so a total of \( O(n^4) \). Next, the Dijkstra algorithm (line 12) has the known time complexity of \( O(n^2) \). Hence the linear CTT-SP algorithm has a worst case time complexity of \( O(n^4) \). Furthermore, the space complexity of the linear CTT-SP algorithm is the space of storing CTT, which is \( O(n^2) \).

From the pseudo-code in Figure 11, we can see that recursive calls (line 14 and line 42) exist in the general CTT-SP algorithm, which makes the algorithm’s complexity highly dependent on the structure of IDG. Next, we analyse the worst case scenario of the algorithm and show that both the time and space complexities are polynomial.

In Figure 11, pseudo-code lines 1 to 21 is for constructing one CTT, i.e. initial CTT. From pseudo-code lines 24 to 50 of the general CTT-SP algorithm, many CTTs are created for the IDG during the process of the Dijkstra algorithm, which determine the algorithm’s computation complexity. The maximum number of the created CTTs is smaller than the number of datasets in the main branch, which is in the magnitude of \( n \). Hence, if we denote the time complexity of the general CTT-SP algorithm as \( F_l(n) \), we have the recursive equation as follows:

\[
\begin{align*}
F_0(n) &= O(n^4) \\
F_l(n) &= n^3 \cdot (F_{l-1}(n_{l-1})) + n^2, \quad l > 0
\end{align*}
\]  

In equation (6), \( n \) is the number of datasets in the IDG, \( n_{l,i} \) is the number of datasets in the sub-branches, and \( l \) is the maximum level of the recursive calls, especially \( F_d(n) \) denotes the situation of linear IDG, where the linear CTT-SP algorithm needs to be called (i.e. pseudo-code in Figure 5).

Intuitively, in equation (6), \( F_d(n) \) seems to have an exponential complexity depending on the level of recursive calls. However, in our scenario, \( F_d(n) \) is polynomial because the recursive call is to find the minimum cost storage strategy of given sub-branches in IDG which has a limited solution space. Hence, we can use the iterative method [28] to solve the recursive equation and derive the computation complexity of the general CTT-SP algorithm.

If we assume that we have already found the minimum cost storage strategies for all sub-branches which means without taking the impact of recursive calls into account, the general CTT-SP algorithm has a time complexity of \( O(n^5) \). Formally, we can transform equation (6) to the following:

\[
\begin{align*}
F_l(n) &= n^3 \cdot (O(1) + n^2) + f_{rec}(F_{l-1}(n_{l-1})) \\
&= O(n^5) + f_{rec}(F_{l-1}(n_{l-1}))
\end{align*}
\]  

In equation (7), function \( f_{rec} \) denotes the complexity of recursive calls, i.e. calculating the minimum cost storage strategies of all sub-branches. Next, we analyse the complexity of recursive calls.

For a sub-branch of a general IDG, given different start dataset and end dataset, its minimum cost storage strategy may be different. Figure 12 shows a sub-branch of IDG with \( w \) datasets. We assume \( d_1 \)’s direct predecessors and \( d_w \)’s direct successors are all stored, then we can calculate a minimum cost storage strategy of the sub-branch. We denote the first stored dataset as \( d_a \) and the last stored dataset as \( d_i \) in the strategy, which is shown in Figure 12. If \( d_1 \)’s adjacent stored predecessors are changed, the minimum cost storage strategy may be different as well. Because
the generation cost of \( d_1 \) is larger than storing the direct predecessors, the first stored dataset in the new strategy must be one of the datasets from \( d_1 \) to \( d_u \). Similarly, if \( d_u \)'s adjacent stored successors are changed, the last stored dataset in the new strategy must be one of the datasets from \( d_u \) to \( d_w \). Hence, given different start and end datasets, a sub-branch of IDG has at most \( u \cdot (w - v) \) different minimum cost storage strategies, which are in the magnitude of \( w^2 \). Similarly, we can prove that for any sub-branches of IDG with \( w \) datasets, there are at most \( w^2 \) different minimum cost storage strategies, given different start and end datasets. Hence, given any sub-branches in IDG at any level of recursive calls, say level \( h \), we have the time complexity \( F_h(w) \cdot w^2 \) of finding all the possible minimum cost storage strategies.

![A sub-branch in IDG](image)

**Figure 12. A sub-branch in IDG**

If we assume that there are \( m \) different sub-branches of recursive calls at level \( h \) that we have to find their minimum cost storage strategies, we have the complexity of recursive calls at this level as follows:

\[
 f_{rec}(F_h(n_h)) \leq \sum_{i=1}^{m} \left( F_h(n_{h,i}) \cdot n_{h,i}^2 \right)
\]

(8)

With formula (8), we can further transform equation (7) and iteratively derive the time complexity of the general CTT-SP algorithm.

Therefore, the entire iteration process from equation (6) is shown as follows:

\[
 F_j(n) = n^5 \left( F_{j-1}(n_{j-1}) + n^2 \right)
\]

\[
 = O(n^5) + f(\eta) \left( F_{j-1}(n_{j-1}) \right) \quad \text{// from(7)}
\]

\[
 \leq O(n^5) + \sum_{i=1}^{m_j} \left( F_{j-1}(n_{j-1,i}) \cdot n_{j-1,i}^2 \right) \quad \text{// from(8)}
\]

\[
 = O(n^5) + \sum_{i=1}^{m_j} \left( n_{j-1,1,1}^3 \left( F_{j-2}(n_{j-2,1,1}) \cdot n_{j-2,1,1}^2 \right) + \sum_{i=1}^{m_{j-2}} \left( F_{j-2}(n_{j-2,1,1}) \cdot n_{j-2,1,1}^2 \right) \right) \quad \text{// recursion}
\]

\[
 \leq O(n^5) + \sum_{i=1}^{m_j} \left( O(n_{j-1,1,1}^3) \cdot n_{j-1,1,1}^2 \right) + \sum_{i=1}^{m_{j-2}} \left( F_{j-2}(n_{j-2,1,1}) \cdot n_{j-2,1,1}^2 \right) \quad \text{// from(7)(8)}
\]

\[
 \leq O(n^5) + \sum_{i=1}^{m_j} \left( O(n_{j-1,1,1}^3) \cdot n_{j-1,1,1}^2 \right) + \cdots + \sum_{i=1}^{m_0} \left( O(n_{0,1}^3) \cdot n_{0,1}^2 \right) \quad \text{// iteration}
\]

\[
 = O(n^5) + \sum_{j=1}^{j} \left( \sum_{i=1}^{m_j} \left( O(n_{j,i}^3) \cdot n_{j,i}^2 \right) \right) + \sum_{i=1}^{m_0} \left( O(n_{0,i}^3) \cdot n_{0,i}^2 \right) \quad \text{// fromF_0(n) = O(n^3)}
\]

\[
 \leq l \cdot m \cdot O(n^5) \cdot n^2 \quad \text{// } m = \max_{i=0}^{j} (m_i)
\]

\[
 \leq O(n^9) \quad \text{// } l < n, \quad m < n
\]

Hence, the worst case time complexity of general CTT-SP algorithm is \( O(n^9) \).

Similarly, the space complexity of general CTT-SP algorithm is \( l \cdot m \cdot n^2 \cdot O(n^5) \), where the worst case is \( O(n^7) \).
5. Evaluation

The on-demand minimum cost benchmarking for intermediate datasets storage strategies proposed in this paper is generic. It can be used in any scientific workflow applications. In this section, we demonstrate the simulation results that we conduct on the SwinCloud system [25]. We start with a description of the simulation environment and strategies. Then we evaluate general (random) workflows to demonstrate the comparison of our benchmark with different storage strategies. Finally, we experiment our algorithm with the specific pulsar searching workflow described in Section 2, and use the real world data to demonstrate how our algorithm finds the minimum cost strategy in storing the intermediate datasets of the pulsar searching workflow.

5.1 Simulation environment and strategies

Figure 13 shows the structure of our simulation environment. SwinCloud is a cloud computing simulation environment built on the computing facilities at Swinburne University of Technology which takes advantage of the existing SwinGrid system [35]. We install VMWare software [7] on SwinCloud, so that it can offer unified computing and storage resources. By utilising the unified resources, we set up data centres that can host applications. In every data centre, Hadoop [5] is installed that can facilitate the MapReduce computing paradigm and distributed data management. SwinDeW-C (Swinburne Decentralised Workflow for Cloud) [25] is a cloud workflow system developed based on SwinDeW [34] and SwinDeW-G [35]. It runs on SwinCloud that can interpret and execute workflows, send and retrieve, save and delete datasets in the virtual data centres. Through a user interface at the application level, which is a Web portal, we can deploy workflows and upload application data to the cloud. In simulations, we facilitate our strategy in SwinDeW-C to manage the intermediate datasets in the simulation cloud.

![Figure 13. Structure of simulation environment](image-url)
To evaluate the performance of our strategy, we run six simulation strategies together and compare the total costs of the system. The strategies are: 1) store all the intermediate datasets in the system; 2) delete all the intermediate datasets, and regenerate them whenever needed; 3) store the intermediate datasets that have high generation cost; 4) store the intermediate datasets that are most often used; 5) dependency based strategy reported in [36] [38], in which we store the datasets by comparing their generation cost rates and storage cost rates; and 6) the minimum cost storage strategy found by the CTT-SP algorithm in our benchmarking.

We have run a large number of simulations with different parameters to evaluate the performance of our benchmark. We evaluate some representative results in this section. More simulation results, as well as the program code, are available at http://www.swinflow.org/docs/Benchmark.zip, where readers can download and view the results and implementation themselves.

5.2 General (random) workflow simulations

To evaluate the overall performance of our strategy in a general manner, we have run a large number of random simulations with the six strategies introduced earlier. In general simulations, we use randomly generated workflows to construct the IDG, and give every intermediate dataset a random size, generation time, usage rate, and then run the workflows under different pricing models. We compare the total system costs over 30 days for different strategies, which show the cost effectiveness of the strategies in comparison to our minimum cost benchmark.

We pick one test case as a representative. In this case, we let the workflow randomly generate 50 intermediate datasets, each with a random size ranging from 100GB to 1TB. The dataset generation time is also random, ranging from 1 hour to 10 hours. The usage rate (time between every usage) is again randomly ranging from 1 day to 10 days. The prices of cloud services follow Amazon clouds’ cost model, i.e. $0.1 per CPU instance-hour for computation and $0.15 per gigabyte per month for storage. We run our algorithm on this IDG to calculate the minimum cost strategy, where 9 of the 50 datasets are chosen to be stored. We use this minimum cost strategy as the benchmark to evaluate the other five strategies introduced in Section 5.1. More random simulation cases can be found from the URL given in Section 5.1.

Figure 14 shows the comparison of the minimum cost benchmark with the strategy of storing high generation cost datasets. We compare the total system costs over 30 days of the strategies that store different percentages of datasets based on the generation cost, and the minimum cost benchmark. The two extreme strategies of storing all the datasets and deleting all the datasets are also included. In Figure 14, we can clearly see the cost effectiveness of different strategies comparing with the benchmark, where storing top 10% generation cost datasets turns out to be the most cost-effective strategy in this case. But the system cost is still much higher than the minimum cost benchmark.

Then we evaluate the storing often used datasets strategy by comparing with the benchmark. We still run simulations of strategies that storing different percentages of datasets based on their usage rates. Figure 15 shows the comparison of the total system costs over 30 days, where we can clearly see the cost effectiveness of different strategies comparing with the benchmark. Also, the strategy of storing top 10% often used datasets turns out to be the most cost-effective one in this case. Comparing to Figure 14, the strategy of storing often used datasets is more cost-effective than storing high generation cost dataset, but it is again still much higher than the minimum cost benchmark.
The intermediate datasets storage strategies reported in [36] [38] are also based on the IDG, which have considered the data dependencies in calculating the datasets’ generation cost and storage cost. Figure 16 shows the comparison of the dependency based strategies with the minimum cost benchmark. In the dependency based static strategy, datasets’ storage statuses are decided when they are first generated in the system by comparing their generation cost rates and storage cost rates, and in the dependency based dynamic strategy, whenever the datasets are regenerated in the system during the runtime, their storage statuses are recalculated and dynamically changed, and other datasets’ storage statuses may also be adjusted accordingly. In Figure 16, we can see that the dependency based strategies have a good performance, which are more cost-effective than the strategies depicted in Figures 14 and 15. Especially for the dynamic strategy, based on the adjustment of the datasets’ storage statuses in the runtime of the system, its cost is close to the minimum cost benchmark that is calculated in the build time.
5.3 Specific pulsar searching workflow simulations

The general (random) workflow simulations demonstrate how to utilise our minimum cost benchmark to evaluate the cost effectiveness of different intermediate datasets storage strategies. Next we utilise it for the specific pulsar searching workflow introduced in Section 2 and show how the benchmark works in the real world scientific application.

In the pulsar example, during the workflow execution, six intermediate datasets are generated. The IDG of this pulsar searching workflow is shown in Figure 17, as well as the sizes and generation times of these intermediate datasets. The generation times are from running this workflow on Swinburne Supercomputer [6], and for simulations, we assume that in the cloud system, the generation times of these intermediate datasets are the same. Furthermore, we also assume that the prices of cloud services follow Amazon clouds’ cost model.

We have run the simulations based on the usage rates of intermediate datasets. From Swinburne astrophysics research group, we understand that the “de-dispersion files” are the most useful intermediate dataset. Based on these files, many accelerating and seeking methods can be used to search pulsar candidates. Based on the scenario, we set the “de-dispersion files” to be used once every 2 days, and the rest of the intermediate datasets to be used once every 5 days. With this setting, we run the above mentioned simulation strategies and calculate the total costs of the system for one branch of the pulsar searching workflow of processing one piece of observation data in 30 days as shown in Figure 18.
From Figure 18 we can see that 1) the cost of the “store all” strategy is a straight line because in this strategy all the intermediate datasets are stored in the cloud storage that is charged at a fixed rate, and there is no computation cost required; 2) the cost of the “store none” strategy is a fluctuated line because in this strategy all the costs are computation cost of regenerating intermediate datasets. For the days that have fewer requests of the data, the cost is low, otherwise, the cost is high; 3-4) the costs of the “store high generation cost datasets” and “store often used datasets” strategies are in the middle band, which are much lower than the “store all” and “store none” strategies. The cost lines are only a little fluctuated, because the intermediate datasets are partially stored; 5-6) the dependency based strategy has a good performance in this pulsar searching workflow, which is very close to the minimum cost benchmark.

Table 1 shows how the six strategies store the intermediate datasets in detail.

<table>
<thead>
<tr>
<th>Strategies</th>
<th>Datasets</th>
<th>Extracted beam</th>
<th>De-dispersion files</th>
<th>Accelerated de-dispersion files</th>
<th>Seek results</th>
<th>Pulsar candidates</th>
<th>XML files</th>
</tr>
</thead>
<tbody>
<tr>
<td>1) Store all</td>
<td>Stored</td>
<td>Stored</td>
<td>Stored</td>
<td>Stored</td>
<td>Stored</td>
<td>Stored</td>
<td>Stored</td>
</tr>
<tr>
<td>2) Store none</td>
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<td>Deleted</td>
<td>Deleted</td>
<td>Deleted</td>
<td>Deleted</td>
<td>Deleted</td>
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</tr>
<tr>
<td>3) Store high generation cost datasets</td>
<td>Deleted</td>
<td>Deleted</td>
<td>Stored</td>
<td>Deleted</td>
<td>Deleted</td>
<td>Deleted</td>
<td>Deleted</td>
</tr>
<tr>
<td>4) Store often used datasets</td>
<td>Deleted</td>
<td>Stored</td>
<td>Deleted</td>
<td>Deleted</td>
<td>Deleted</td>
<td>Deleted</td>
<td>Deleted</td>
</tr>
<tr>
<td>5) Dependency based strategy</td>
<td>Deleted</td>
<td>Stored (deleted initially)</td>
<td>Deleted</td>
<td>Stored</td>
<td>Deleted</td>
<td>Deleted</td>
<td>Stored</td>
</tr>
<tr>
<td>6) Minimum cost benchmark</td>
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<td>Deleted</td>
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<td>Stored</td>
</tr>
</tbody>
</table>

Since the intermediate datasets of this pulsar searching workflow is not very complicated, we can do some intuitive analyses on how to store them. For the accelerated de-dispersion files, although its generation cost is quite high, comparing to its huge size, it is not worth storing them in the cloud. However, in the strategy of “store high generation cost datasets”, the accelerated de-dispersion files are chosen to be stored. For the final XML files, they are not very often used, but comparing to the high generation cost and small size, they should be stored. However, in the strategy of “store often used datasets”, these files are not chosen to be stored. For the de-dispersion files, by comparing their own generation cost rate and storage cost rate, the
dependency based strategy does not store them at the beginning, but store them after they are used in the regeneration of other datasets.

6. Related work

Comparing to the distributed computing systems like cluster and grid, a cloud computing system has a cost benefit [10]. Assunção et al. [11] demonstrate that cloud computing can extend the capacity of clusters with a cost benefit. Using Amazon clouds’ cost model and BOINC volunteer computing middleware, the work in [24] analyses the cost benefit of cloud computing versus grid computing. The idea of doing science on the cloud is not new. Scientific applications have already been introduced to cloud computing systems. The Cumulus project [32] introduces a scientific cloud architecture for a data centre, and the Nimbus [23] toolkit can directly turns a cluster into a cloud which has already been used to build a cloud for scientific applications. In terms of the cost benefit, the work by Deelman et al. [19] also applies Amazon clouds’ cost model and demonstrates that cloud computing offers a cost-effective way to deploy scientific applications. The above works mainly focus on the comparison of cloud computing systems and the traditional distributed computing paradigms, which shows that applications running on the cloud have cost benefits. However, our work studies how to reduce the cost if we run scientific workflows on the cloud. In [19], Deelman et al. present that storing some popular intermediate data can save the cost in comparison to always regenerating them from the input data. In [8], Adams et al. propose a model to represent the trade-off of computation cost and storage cost, but have not given the strategy to find this trade-off. In [36] [38], Yuan et al. propose a cost-effective strategy for intermediate data storage in scientific cloud workflows systems that takes data dependency into consideration. Comparison with the benchmark proposed in this paper indicates that the strategy in [36] [38] has a good performance, but does not achieve the minimum cost of the system. In this paper, the minimum cost benchmarking contains an innovative algorithm (i.e. CTT-SP algorithm) that can find the minimum cost strategy on demand for storing intermediate datasets in scientific cloud workflow systems based on the historic usage information of the datasets.

The study of data provenance is important for our work. Due to the importance of data provenance in scientific applications, much research about recording data provenance of the system has been done [21] [12]. Some of them are especially for scientific workflow systems [12]. Some popular scientific workflow systems, such as Kepler [26], have their own system to record provenance during the workflow execution [9]. In [30], Osterweil et al. present how to generate a Data Derivation Graph (DDG) for the execution of a scientific workflow, where one DDG records the data provenance of one execution. Similar to the DDG, our IDG is also based on the scientific workflow data provenance, but it depicts the dependency relationships of all the intermediate data in the system. With the IDG, we know where the intermediate data are derived from and how to regenerate them.

7. Discussion

As cloud computing is such a fast growing market, different cloud service providers will appear. In the future, we will be able to flexibly select service providers to conduct our applications based on their pricing models. An intuitive idea is to incorporate different cloud service providers in our applications, where we can store the data with the provider who has a lower price in storage resources, and choose the provider who has lower price of computation
resources to run the computation tasks. However, at present, normally it is not practical to run scientific applications among different cloud service providers because of the following reasons:

1) The data in scientific applications are usually very large in size. They are too large to be transferred efficiently via the Internet. Due to bandwidth limitations of the Internet, in today’s scientific projects, delivery of hard disks is a common practice to transfer application data, and it is also considered to be the most efficient way to transfer terabytes of data [10]. Nowadays, express delivery companies can deliver the hard disks nation wide by the end of the next day and world wide in 2 or 3 days. In contrast, transferring one terabyte data via the Internet would take more than 10 days at a speed of 1MB/s. To break the bandwidth limitation, some institutions set up dedicated fibres to transfer data. For example, Swinburne University of Technology has built a fibre to Parkes with gigabit bandwidth. However, it is mainly used for transferring gigabytes of data. To transfer terabytes of data, scientists would still prefer to ship hard disks. Furthermore, building fibre connections is expensive, and they are not yet wildly used in the Internet. Hence, transferring scientific application data between different cloud service providers via the Internet is not efficient.

2) Cloud service providers place high cost on data transfer in and out their data centres. In contrast, data transfer within one cloud service provider’s data centres are usually free. For example, the data transfer price of Amazon cloud service is: $0.1 per GB of data transferred in and $0.17 per GB of data transferred out. Compared to the storage price of $0.15 per GB per month, the data transfer price is relatively high, such that finding a cheaper storage cloud service provider and transferring data may not be cost effective. In cloud service providers’ position, they charge high price on data transfer not only because of the bandwidth limitation, but also as a business strategy. As data are deemed as an important resource today, cloud service providers want users to keep all the application data in their storage cloud. For example, Amazon made a promotion that placed a zero price on data transferred into its data centres, until June 30, 2010, which means users could upload their data to Amazon’s cloud storage for free. However, the price of data transfer out of Amazon is still the same.

Given the two reasons discussed above, the most efficient and cost-effective way to run scientific applications in the cloud is to keep all the data and run the applications with one cloud service provider, where the similar conclusion is also stated in [19]. Hence, in the strategy stated in this paper, we did not take data transfer cost into consideration. However, some scientific applications may have to run in a distributed manner [16] [15], because the required datasets are distributed, some with fixed locations. In these cases, data transfer is inevitable, and data placement strategy [37] would be needed to reduce the data transfer cost.

8. Conclusions and Future Work

In this paper, based on an astrophysics pulsar searching workflow, we have examined the unique features of intermediate datasets storage in scientific cloud workflow systems and developed a novel algorithm that can find the minimum cost intermediate datasets storage strategy on demand. This strategy achieves the best trade-off of computation cost and storage cost of the cloud resources, which can be utilising as the minimum cost benchmark for evaluating the cost effectiveness of other datasets storage strategies. Simulation results of both general (random) workflows and the specific pulsar searching workflow demonstrate that our benchmarking serves well for such a purpose.
Our current work is based on Amazon clouds’ cost model and assumes that all the application data are stored with a single cloud service provider. However, sometimes scientific workflows have to run in a distributed manner since some application data are distributed and may have fixed locations. In these cases, data transfer is inevitable. In the future, we will further develop some data placement strategies in order to reduce data transfer among data centres. Furthermore, to widely utilise our benchmarking, models of forecasting intermediate datasets usage rate can be further studied. It must be flexible in order to be adapted to different scientific applications. Due to the dynamic nature of cloud computing environment, the minimum cost benchmarking of scientific cloud workflows needs to be enhanced, where the minimum cost benchmark should be able to dynamically adjust according to the change of datasets usages at runtime.

Acknowledgement

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